

KURTOSIS DPLL AND PTCM DECODER FOR NON-LINEARLY AMPLIFIED 16-QAM

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ABSTRACT

We describe a non-decision directed kurtosis-based digital phase lock loop (DPLL) algorithm for 16-QAM carrier recovery in the presence of non-linear amplification. A constellation rotation (with respect to locked phase) allows each of the trellis decoder's set-partitions to be fully confined to the received vector quadrants. Transponder characteristic variations may be automatically tracked by adapting the TCM decoder's metric LUT based on 4 dominant maxima in a 2-D histogram of quadrant data.

INTRODUCTION

Operated near saturation from efficiency considerations, satellite transponder distortion of a high-order modulation (HOM) degrades performance of a receiver that presumes an undistorted constellation. For example, satcom standards such as [1, 2] use 16-QAM modulation (see Figure 1) together with inner pragmatic trellis coded modulation (PTCM), relying on an "industry standard" constraint length 7, rate $\frac{1}{2}$, convolutional code, and a Reed-Solomon outer code over $GF(2^8)$.

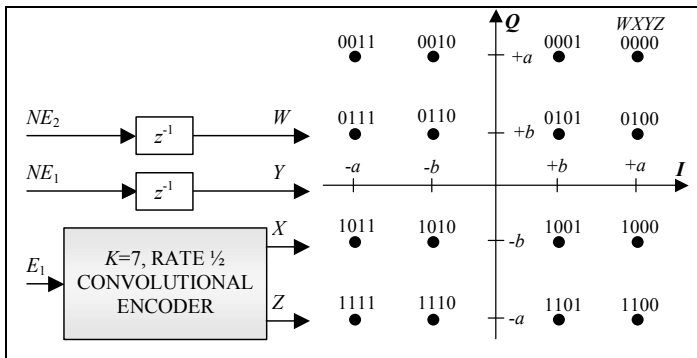


Figure 1. 16-QAM PTCM and constellation mapping (not $n \cdot \pi/2$ rotationally invariant)

For a general 16-QAM, the constellation points $I+jQ$ allow $I = \pm a, \pm b, Q = \pm a, \pm b$, yielding a signal power, $S = a^2 + b^2$ and three possible IF signal amplitudes: $\sqrt{2} \cdot b$, $(a^2 + b^2)^{0.5}$ and $\sqrt{2} \cdot a$. With an unequally-spaced constellation, e.g., $a = \pm \cos(\pi/8)$ and $b = \pm \sin(\pi/8)$, the peak-to-rms ratio of carrier-modulated 16-QAM is $2 \cdot a \cdot (a^2 + b^2)^{-0.5} = 2 \cdot \cos(\pi/8)$ (i.e., 5.33dB at carrier; 2.33dB at baseband).

Two methods of mitigating non-linear amplification effects of satellite transponders on HOMs are:

- Transmit-side pre-distortion [3,4], requiring prior knowledge of satellite transponder characteristics (that are presumed predictable with respect to operating temperature and aging)
- Receive-side mitigation techniques include, among others, equalization based on a Volterra expansion of the non-linear channel [5,6] and decision feedback [7]

We describe two variations to [7]'s receive-side mitigation, that improve 16-QAM TCM decoder performance in the presence of:

- Recovered carrier phase noise
- Non-linear phase (w.r.t. frequency) response of analog (e.g., low insertion loss SAW) filters
- Varying (e.g., w.r.t. temperature and age) non-linear power amplifier phase and amplitude response.

In this paper's next section, [7]'s TCM decoder based decision-directed¹ phase/ amplitude vector tracker is omitted² in favor of low-complexity, non-decision directed kurtosis computations (briefly described in [8]) that allow the receiver's DPLL to adapt automatically (and independent of TCM decoder) to the transponder's (potentially varying) input amplitude-dependent phase and amplitude responses. Prior work on blind QAM carrier phase tracking, either for dispersive channels [9], or additive-noise, non-dispersive channels (raising received data to the 4th power and then determining concentration ellipse orientation) [10], have not been extended to the memory-less non-linear satellite channel.

In the subsequent section, maximum likelihood (ML) vectors, for each of the three 16-QAM constellation's amplitudes, are recovered from four dominant peaks in a 2-D histogram of received vectors (each rotated into the first quadrant) in order to update the trellis decoder's metric

¹ A decision-directed PLL's (DDPLL's) initial convergence rate depends upon the deviation of the actual transponder's characteristic from an initially presumed default (which is updated as the system learns); a non-decision directed approach achieves rapid phase-lock without making any assumptions on transponder AM-AM or AM-PM response.

² It may be advantageous, e.g., with more advanced coding schemes, to take a combined approach where a kurtosis DPLL is used during acquisition and the decision-directed approach of [7] during tracking.

look-up table (LUT), reducing, when compared to the sub-domain centroids method of [7], centrifugal displacement, at low SNR, of the four estimated vectors from the actual transmit vectors.

Experimental results and conclusions are provided in the paper's final sections.

NON DECISION-DIRECTED DPLL FOR NON-LINEARLY AMPLIFIED 16-QAM

A non decision-directed DPLL for undistorted 16-QAM (of Figure 1) may be based on the phase dependence of kurtosis of either channel (say, Q), with $S=a^2+b^2$ and $\rho=b/a$, $\kappa=[\rho/(1+\rho^2)]^2$ according to (with $A=1.875$ and $B=0.375$ for no-noise³ case):

$$\begin{aligned} \frac{E[Q^4]}{E[Q^2]^2} &= \left[\frac{9}{4} + 3 \cdot \kappa \cdot \left(\frac{2N}{S} - 1 \right) \right] - \left[\left(\frac{1}{4} + \kappa \right) \cdot \left(1 - \frac{2N}{S} \right) \right] \cdot \cos[4(\phi + \psi)] \\ &= A - B \cdot \cos[4(\phi + \psi)] \end{aligned} \quad (1)$$

A band-limited, reduced peak-to-rms, 16-QAM modulation is achieved either by pulse shaping a pre-distorted constellation or by RF bandlimiting of non-linearly amplified 16-QAM signal (avoiding spectral regrowth beyond a stipulated spectral mask). For a TWTA, the Saleh model [11] baseband amplitude (AM-AM) and phase (AM-PM) responses are $A(r)=\alpha_a \cdot r/(1+\beta_a \cdot r^2)$ and $\phi(r)=\alpha_\phi \cdot r^2/(1+\beta_\phi \cdot r^2)$ respectively as shown in Figure 2. Typical parameter values are $\alpha_a=2.0$, $\beta_a=1.0$, $\alpha_\phi=2.5$ and $\beta_\phi=2.8$.

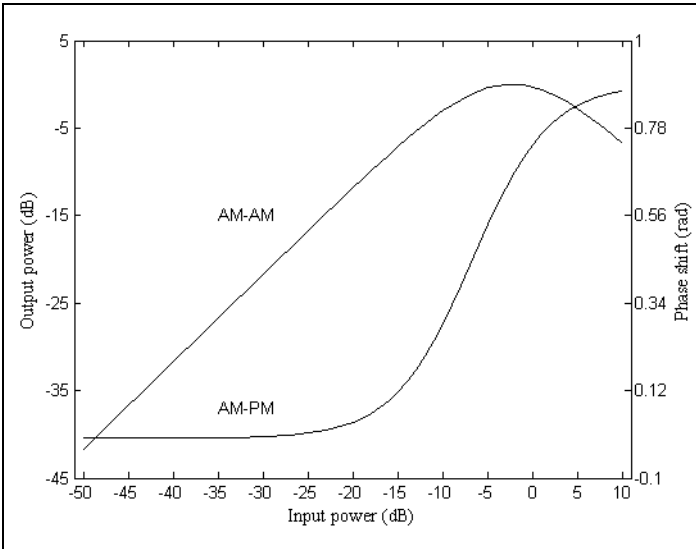


Figure 2. Typical TWTA AM-AM and AM-PM model

For GaAsFETs, the Ghorbani [12] model for AM-AM distortion, with $A(r)=[(x_1 \cdot r^{x_2})/(1+x_3 \cdot r^{x_3})]+x_4 \cdot r$, may be used while Saleh's AM-PM distortion retained to obtain a 6 (rather

³ 16-QAM TCM with outer Reed-Solomon coding (as per [1]), at operating SNR, has $2 \cdot N/S \approx 0.08$; i.e., the high-backoff bias of A , due to neglecting (1)'s SNR dependence, is only 1% of its no-noise value.

than Ghorbani's 8) parameter model. Typical parameters are $x_1=8$, $x_2=1.5$, $x_3=6.5$, $x_4=-0.1$, $\alpha_\phi=5.5$ and $\beta_\phi=13$. The AM-AM for SSPA [13] model is $A(r)=r/[1+r/(\alpha_a)]^{0.5}$ while $\phi(r)=0$, with $\alpha_a=0.4$. Figure 3 shows the kurtosis vs. phase relationship for typical SSPA, TWTA and GaAsFET amplifier characteristics, which is of the form $A - B \cdot \cos[4(\phi + \psi)]$, where ψ , a phase offset, aligns all sub-constellations' centroids with the $\pm 45^\circ$ axes.

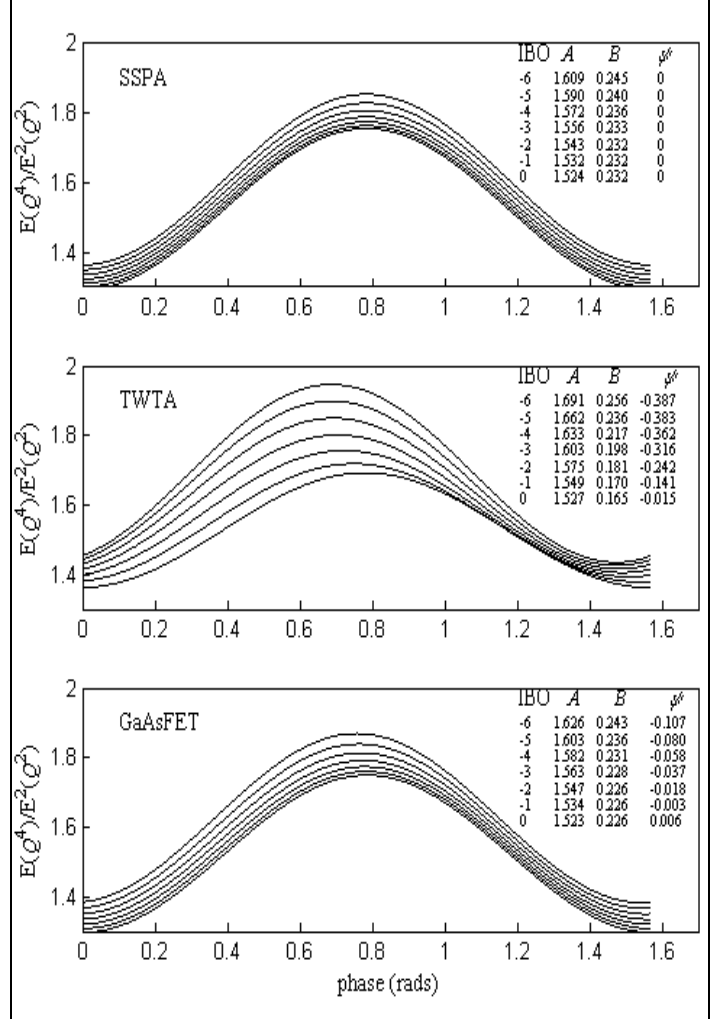


Figure 3. Kurtosis as a function of phase for typical SSPA, TWTA and GaAsFET amplifiers

$E[R^4]/E^2[R^2] = \{E[Q^4] + E[I^2 Q^2]\} / \{2 \cdot E^2[Q^2]\}$ determines⁴ A . Irrespective of distortion, phase can be locked near $\phi =$

$$\begin{aligned} \frac{E[I^2 Q^2]}{E^2[Q^2]} &= \left[\frac{3}{4} + \kappa \cdot \left(\frac{2 \cdot N}{S} - 1 \right) + \frac{N}{2 \cdot S} \right] + \left[\left(\frac{1}{4} + \kappa \right) \cdot \left(1 - \frac{2 \cdot N}{S} \right) \right] \cdot \cos[4(\phi + \psi)] \\ &= \frac{A}{3} - B \cdot \cos[4(\phi + \psi)] \end{aligned}$$

e.g., A , computed as $1.5 \cdot E[R^4]/E^2[R^2]$, has a high-backoff bias of 0.375 $\cdot (N/S)$ ($\approx 0.8\%$ of (1)'s 1st term value at a 14dB operating SNR).

$\pi/8^5$ using Figure 4's DPLL structure⁶. A kurtosis-based DPLL, while requiring the same AGC (and kurtosis) settling time as a DDPLL, has the following advantages:

- A kurtosis-based DPLL can achieve rapid phase-lock without making symbol decisions as opposed to a DDPLL that slowly adapts its decision boundaries to an unknown transmit back-off
- A block kurtosis estimate reuses partial block computations of other modules (e.g., AGC)

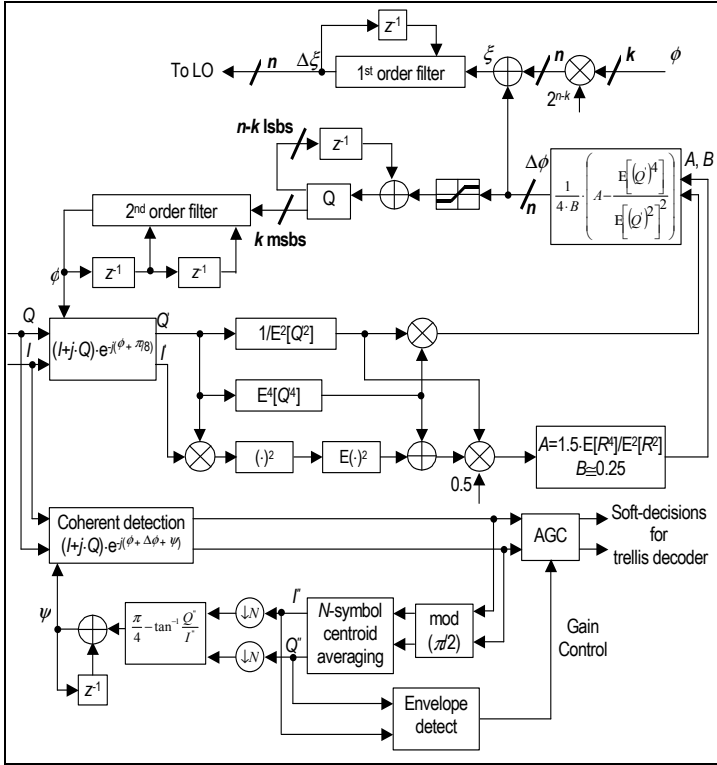


Figure 4. Kurtosis DPLL for 16-QAM; $n > k$

Even after the kurtosis-based DPLL is locked, a phase offset (with respect to aligning sub-constellations' centroids to the $\pm 45^\circ$ axes), ψ , exists due to the non-linear amplifier's AM/PM characteristic (as Figure 5 shows); ψ , computed as the difference between $\pi/4$ and the averaged centroids' argument⁷ (modulo 90°), corrects this phase offset (together with any residual DPLL phase offset).

⁵ When A is presumed (as a default on power-on, as the previous value otherwise) in burst mode, phase variations w.r.t. IBO are smaller at $-\pi/8$ (as compared to $\pi/8$).

⁶ Using a smaller than true value for B increases DPLL phase noise, while selecting a larger B , such as 0.25 (see Figure 4), may result in a residual phase offset; however, this phase offset gets included in ψ .

⁷ From Figure 5, $(x_1, y_1) = \left(\frac{\sqrt{2} \cdot b \cdot \alpha_a}{1 + 2 \cdot b^2 \cdot \beta_a} \right) \cdot e^{j \left[\frac{\pi}{4} + \frac{2 \cdot b^2 \cdot \alpha_\phi}{1 + 2 \cdot b^2 \cdot \beta_\phi} \right]}$

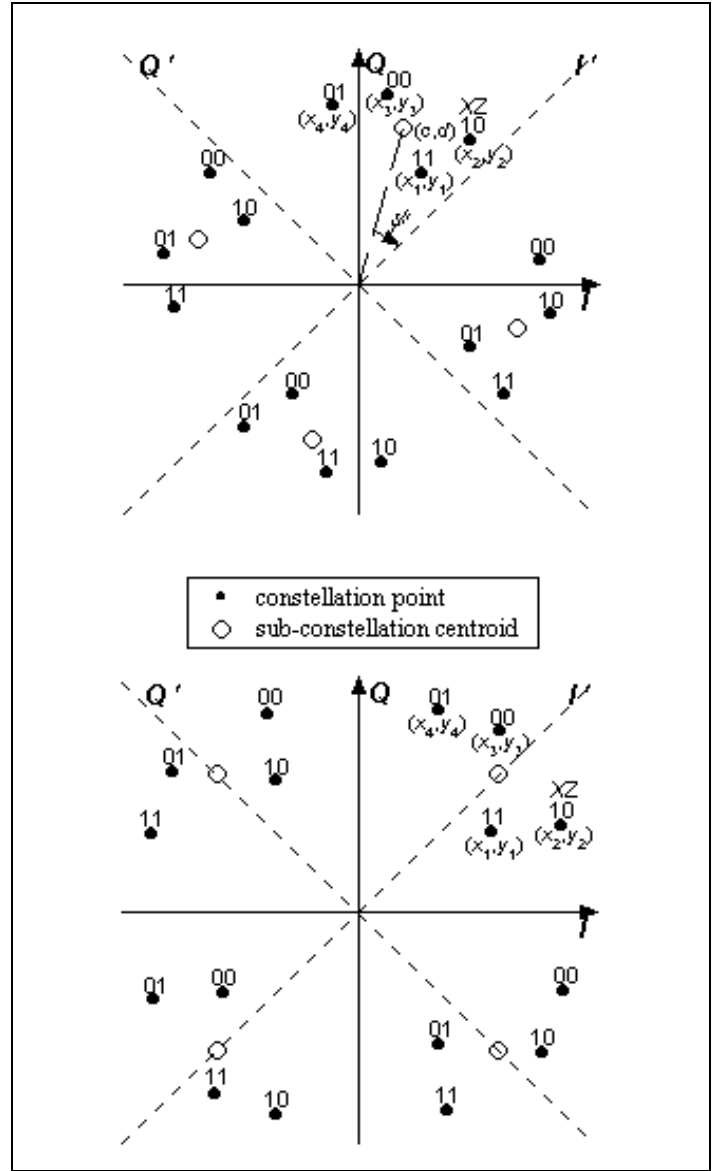


Figure 5. 16-QAM phase recovery (top) and rotated constellation presented to trellis decoder (bottom) The AGC, initially controlled (as for constant envelope modulations) by $S+N$, is controlled by the averaged centroid modulus after phase lock, in order that the gain-

$$(x_2, y_2) = \left(\frac{\alpha_a \cdot \sqrt{a^2 + b^2}}{1 + (a^2 + b^2) \cdot \beta_a} \right) \cdot e^{j \left[\tan^{-1} \left(\frac{b}{a} \right) + \frac{\alpha_\phi (a^2 + b^2)}{1 + (a^2 + b^2) \beta_\phi} \right]}$$

$$(x_3, y_3) = \left(\frac{\sqrt{2} \cdot a \cdot \alpha_a}{1 + 2 \cdot a^2 \cdot \beta_a} \right) \cdot e^{j \left[\frac{\pi}{4} + \frac{2 \cdot a^2 \cdot \alpha_\phi}{1 + 2 \cdot a^2 \cdot \beta_\phi} \right]}$$

$$(x_4, y_4) = \left(\frac{\alpha_a \cdot \sqrt{a^2 + b^2}}{1 + \beta_a \cdot (a^2 + b^2)} \right) \cdot e^{j \left[\tan^{-1} \left(\frac{a}{b} \right) + \frac{\alpha_\phi (a^2 + b^2)}{1 + \beta_\phi (a^2 + b^2)} \right]}$$

Thus, the centroid $(c, d) = 0.25 \cdot (x_1 + x_2 + x_3 + x_4, y_1 + y_2 + y_3 + y_4)$

compensated sub-constellations' centroids have a constant modulus at the trellis decoder's input.

16-QAM PTCM DECODING

Without distortion, each 16-QAM PTCM symbol is decoded, producing 3 bits per symbol, using very few additional computations over the underlying rate $\frac{1}{2}$, constraint length 7, Viterbi decoder. We retain a low-complexity decoder for non-linearly amplified 16-QAM as well.

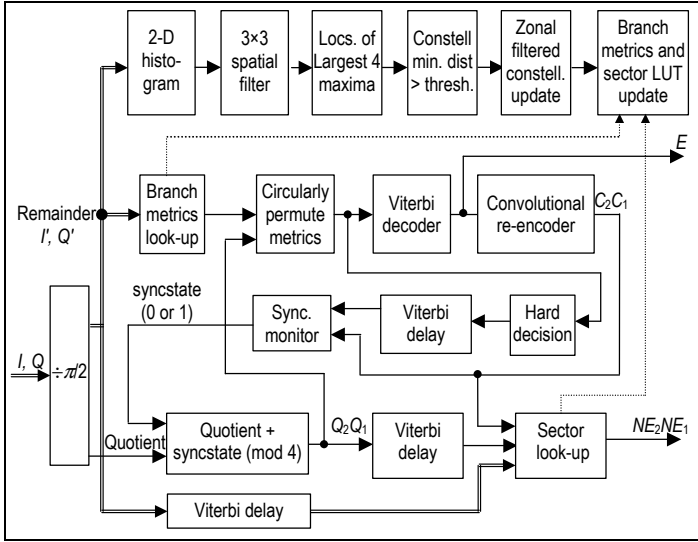


Figure 6. 16-QAM-Trellis decoder block diagram

In Figure 6, received I/Q vectors are rotated by $m \cdot \pi/2$, $m = \lfloor 2 \cdot \arg(I+jQ)/\pi \rfloor$, to obtain I'/Q' vectors, that address the 1st quadrant Viterbi branch metrics LUT. These metrics are then circularly permuted, based on m , prior to being fed to the Viterbi decoder. Comparing the mismatches in delayed hard decisions and convolutionally re-encoded Viterbi output with a threshold indicates the decoder's synchronization state (a 90° phase rotation allowing synchronization⁸ in the event of failure). Finally, the 1st quadrant non-encoded bits, obtained by using I'/Q' to index the sector LUT, are re-mapped to the m -th quadrant. In parallel, branch-metric and sector LUTs are updated by finding 4 dominant maxima in a spatially filtered 2-D histogram, averaged over a suitable period, of I'/Q' vectors. Minimum intra-constellation distance thresholding and constellation change zonal filtering prevents the LUTs from ever being contaminated by erroneously estimated signal sets. Measured E_b/N_0 (with distortion) may be used to calibrate the E_b/N_0 estimate provided by the rate-3/4 16-QAM TCM decoder, which is based on all quadrants' 4-QAM hard-decision error rate⁹.

⁸ Unique-word based outer (e.g., Reed-Solomon) code frame synchronizer resolves 180° phase ambiguity

⁹ For 4-QAM with $P_b \approx Q[(0.5 \cdot d_{\min}^2/N_0)^{0.5}] > 0.5 \cdot \text{erfc}[(E_b/N_0)^{0.5}]$; at high SNR, $P_b > 0.25 \exp[-0.5 \cdot (E_b/N_0)]$. A correction (via calibration) to esti-

EXPERIMENTAL RESULTS

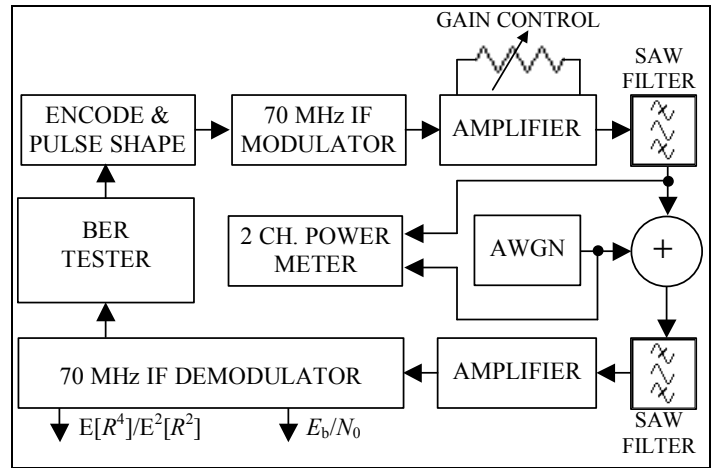


Figure 7. 16-QAM performance testing w.r.t. distortion

The set-up of Figure 7 measures distortion-adaptive demodulator performance. An attenuator sets the modulator amplifier's IBO, while the demodulator's $E[R^4]/E^2[R^2]$ infers IBO. Figure 8 shows unsaturated and saturated 16-QAM performance, each with its associated constellation. ML-derived constellations are not centrifugally displaced, while domain-derived centroids are.

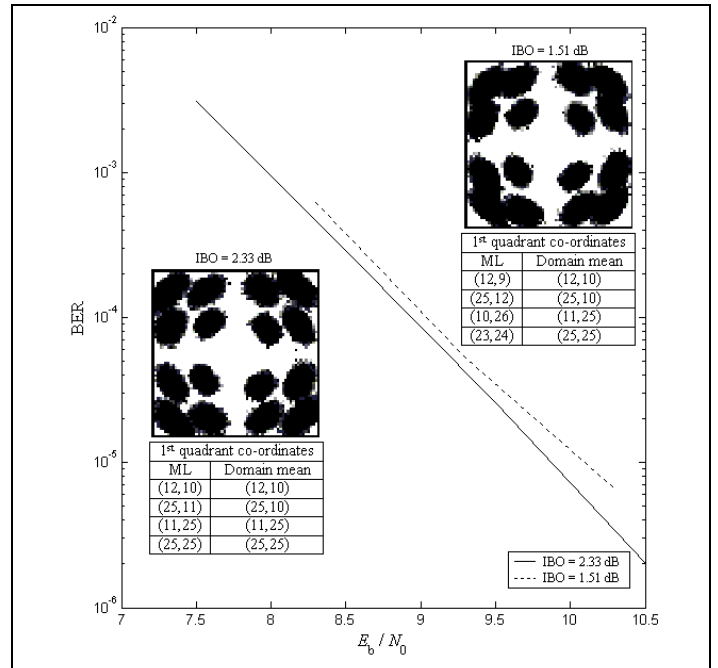


Figure 8. $b/a=0.414$ 16-QAM performance with 2.33 and 1.51dB IBO's; symbol-time bandwidth product $(B \cdot T_s)=1$

imated E_b/N_0 (with distortion) is made because, in dB, $(E_b/N_0)_{4\text{-QAM}} > 10 \cdot \log_{10}[-2 \cdot \ln(4 \cdot P_b)]$ and $(E_b/N_0)_{16\text{-QAM}} = 6.58 + (E_b/N_0)_{4\text{-QAM}}$.

CONCLUSIONS

Optimum 16-QAM demodulator performance on diverse satellite channels (e.g., using SSPA, TWTA, or GaAsFET power amplifiers) is obtained via:

- A robust and computationally efficient non-decision directed DPLL for fast phase and frequency acquisition
- Unambiguous subset (quadrant) partitioning/ labeling
- TCM decoder LUT update based on 4 dominant maxima in a 2-D histogram of quadrant data

While kurtosis DPLL expressions and constellation recovery remain identical for non-square (NS) 8-QAM [14], other (higher order) QAMs, as well as other codes (e.g., LDPC), can be processed with a similar methodology. Though the non-decision directed DPLL described here provides good performance for the particular 16-QAM/TCM considered, it may be advantageous to use non-decision directed DPLL during acquisition and the decision directed approach of [7] during tracking for other modulations and codes (e.g. [14]).

REFERENCES

[1] EN 301 210 *Digital Video Broadcasting (DVB); Framing structure, channel coding and modulation for Digital Satellite News Gathering (DSNG) and other contribution applications by satellite*, v1.1.1 (1999-03).

[2] *Intelsat Earth Station Standards (IESS)*, Document IESS-316, Performance characteristics for digital carriers using 16-QAM modulation, October 24, 2003

[3] G. Karam and H. Sari, "Analysis of predistortion, equalization, and ISI cancellation techniques in digital radio systems with nonlinear transmit amplifiers," *IEEE Trans. Commun.*, vol. 37, pp. 1245-1252, December 1989.

[4] G. Karam and H. Sari, "A data predistortion technique with memory," *IEEE Trans. Commun.*, vol. 39, pp. 336-344, February 1991.

[5] S. Benedetto, E. Biglieri and R. Daffara, "Modeling and performance evaluation of nonlinear satellite links – a Volterra series approach," *IEEE Trans. Aerosp. Electron. Syst.*, vol. 15, pp. 494-507, July 1979.

[6] S. Benedetto and E. Biglieri, "Nonlinear equalization of digital satellite channels," *IEEE J. Select. Areas Commun.*, vol. 1, pp. 57-62, January 1983.

[7] R. De Gaudenzi and M. Luise, "Analysis and design of all-digital demodulator for trellis-coded 16-QAM transmission over a nonlinear satellite channel," *IEEE Trans. Commun.*, vol. COM-43, pp. 659-667, Feb.-Apr., 1995.

[8] S. Jayasimha, P. Jyothendar and S. Pavanalatha, "SDR Framework for burst/continuous MPSK/ 16-QAM modems," Proc. of *SPCOM '04*, ISBN 0-7803-8675-2, IEEE catalog no. 04EX926C.

[9] A. Belouchrani and W. Ren, "Blind carrier phase tracking with guaranteed global convergence," *IEEE Trans. on Sig. Proc.*, vol. 45, pp. 1889-1894, July 1997.

[10] P. Campisi et. al, "Blind Phase Recovery for QAM Communication Systems," *IEEE Trans. on Sig. Proc.*, vol. 53, pp. 1348-1357, April 2005.

[11] A. A. M. Saleh, "Frequency-independent and frequency-dependent nonlinear models of TWT amplifiers," *IEEE Trans. Commun.*, vol. COM-29, pp. 1715-1720, November, 1981.

[12] A. Ghorbani and M. Sheikhan, "The effect of Solid State Power Amplifiers (SSPAs) Nonlinearities on MPSK and M-QAM Signal Transmission", *Sixth Int'l Conference on Digital Processing of Signals in Comm.*, 1991, pp. 193-197.

[13] R. Nee and R. Prasad, *OFDM for Wireless Multimedia Communications*, Artech House Publishers, 2000.

[14] L. Li, D. Divsalar and S. Dolinar, "Iterative Demodulation, Demapping and Decoding of Coded Non-Square QAM," *IEEE Trans. Commun.*, vol. 53, pp. 16-19, Jan., 2005.